

## Term Information

Effective Term Autumn 2016  
*Previous Value* Summer 2012

## Course Change Information

### What change is being proposed? (If more than one, what changes are being proposed?)

We propose to change Math 6501 and 6502 from 5-credit to 3-credit courses. We also are taking the opportunity to update the syllabus for each course to a more modern combinatorics curriculum. Moreover, old references to quarter courses are eliminated.

### What is the rationale for the proposed change(s)?

Almost all of our 6000-level courses are 3-credit courses. We hope that this will resolve scheduling issues which we have had in recent years, and also problems with low enrollment. We are also happy to update the curriculum to reflect current research areas of broad interest and applications of interest to PhD students in engineering disciplines and theoretical computer science. This is in part also motivated by several recent faculty hires in the area.

### What are the programmatic implications of the proposed change(s)?

(e.g. program requirements to be added or removed, changes to be made in available resources, effect on other programs that use the course)?

This will not change any program requirements. However, we hope that it will make it easier for PhD students to satisfy a breadth requirement by taking the 6501-6502 sequence, and also expedite PhD students in combinatorics and discrete mathematics to their research programs.

Is approval of the request contingent upon the approval of other course or curricular program request? No

Is this a request to withdraw the course? No

## General Information

Course Bulletin Listing/Subject Area Mathematics  
Fiscal Unit/Academic Org Mathematics - D0671  
College/Academic Group Arts and Sciences  
Level/Career Graduate  
Course Number/Catalog 6502  
Course Title Combinatorics and Graph Theory II  
Transcript Abbreviation Combin Graph Thy 2  
Course Description Ramsey theory, extremal graph theory. First moment method, second moment method, alterations. Concentration inequalities. Lovasz local lemma. Martingale methods. Correlation inequalities. Phase transitions. Random trees, random planar maps.  
*Previous Value* *Combinatorial designs and geometries; coding theory; enumeration, Moebius inversion and Polya theory; algebraic graph theory, spectrum of graphs; association schemes; combinatorics of the symmetric groups; generating functions and q-series.*  
Semester Credit Hours/Units Fixed: 3  
*Previous Value* *Fixed: 5*

## Offering Information

Length Of Course 14 Week  
Flexibly Scheduled Course Never  
Does any section of this course have a distance education component? No  
Grading Basis Letter Grade  
Repeatable No  
Course Components Lecture

|                            |          |
|----------------------------|----------|
| Grade Roster Component     | Lecture  |
| Credit Available by Exam   | No       |
| Admission Condition Course | No       |
| Off Campus                 | Never    |
| Campus of Offering         | Columbus |

## Prerequisites and Exclusions

|                                |   |
|--------------------------------|---|
| Prerequisites/Corequisites     | Math 6501 or permission of instructor     |
| <a href="#">Previous Value</a> | <a href="#">6501 (776)</a> .              |
| Exclusions                     |   |
| <a href="#">Previous Value</a> | Not open to students with credit for 777. |

## Cross-Listings

Cross-Listings

## Subject/CIP Code

|                  |                 |
|------------------|-----------------|
| Subject/CIP Code | 27.0102         |
| Subsidy Level    | Doctoral Course |
| Intended Rank    | Doctoral        |

## Requirement/Elective Designation

The course is an elective (for this or other units) or is a service course for other units

## Course Details

|  |   |
|--|---|
| Course goals or learning objectives/outcomes | <ul style="list-style-type: none"><li>• This course is meant to introduce graduate students to probabilistic combinatorics. An emphasis is placed on covering the fundamentals of these subjects at a fast pace, emphasizing areas which are important for applications.</li></ul>  |
| <a href="#">Previous Value</a>               |   |
| Content Topic List                           | <ul style="list-style-type: none"><li>• Ramsey theory, extremal graph theory.</li><li>• First moment method, second moment method, alterations.</li><li>• Concentration inequalities.</li><li>• Lovasz local lemma.</li><li>• Martingale methods.</li><li>• Correlation inequalities &amp; Phase transitions.</li><li>• Random trees, random planar maps.</li></ul> |

**Previous Value**

- [Combinatorial designs and geometries](#)
- [Coding theory](#)
- [Enumeration, including Moebius inversion and Polya theory](#)
- [Algebraic graph theory and spectrum of graphs](#)
- [Association schemes](#)
- [Combinatorics of the symmetric groups](#)
- [Generating functions and q-series](#)

**Attachments**

- MATH\_6502\_Ed\_Syllabus.pdf: 6502 Syllabus  
*(Syllabus. Owner: Kerler, Thomas)*
- MATH\_6502\_OLD\_Syllabus.pdf: OLD 6502 Syllabus  
*(Syllabus. Owner: Kerler, Thomas)*

**Comments**

- Please also attach 5-credit syllabus of 6502 for comparison. *(by Vankeerbergen, Bernadette Chantal on 12/04/2015 12:16 PM)*

**Workflow Information**

| Status             | User(s)   | Date/Time           | Step                   |
|--------------------|---|---------------------|------------------------|
| Submitted          | Kerler, Thomas  | 12/01/2015 01:52 PM | Submitted for Approval |
| Approved           | Husen, William J  | 12/01/2015 01:57 PM | Unit Approval          |
| Approved           | Haddad, Deborah Moore   | 12/01/2015 03:15 PM | College Approval       |
| Revision Requested | Vankeerbergen, Bernadette Chantal   | 12/04/2015 12:22 PM | ASCCAO Approval        |
| Submitted          | Kerler, Thomas  | 12/05/2015 06:30 PM | Submitted for Approval |
| Approved           | Husen, William J  | 12/05/2015 06:46 PM | Unit Approval          |
| Approved           | Haddad, Deborah Moore   | 12/05/2015 07:36 PM | College Approval       |
| Pending Approval   | Nolen, Dawn<br>Vankeerbergen, Bernadette Chantal<br>Hanlin, Deborah Kay<br>Jenkins, Mary Ellen Bigler<br>Hogle, Danielle Nicole | 12/05/2015 07:36 PM | ASCCAO Approval        |

# Combinatorics and Graph Theory II

## Instructor and Class Information

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Lecturer:

Course Num.:

Office:

Lecture Room:

Phone:

Lecture Times:

Email:

Office Hours:

## About Course Goals

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### FORMAT

The course will meet three times a week for 55 minutes each meeting. Instructions will be mainly by lecture delivered by the instructor. It may also include occasional in-class discussion as well as short student presentations, particularly, by post-candidacy students.

### CONTENT & GOALS

This course is meant to introduce graduate students to probabilistic combinatorics. An emphasis is placed on covering the fundamentals of these subjects at a fast pace, emphasizing areas which are important for applications. Many open problems and areas of current research will be pointed out along the way.

### PREREQUISITES

Math 6501 or permission of instructor

## Textbook

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### MAIN REFERENCE

Noga Alon and Joel Spencer: *The Probabilistic Method: Third Edition*. Wiley, 2008. ISBN: 978-0470170205

## Assessments

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### HOMEWORK ASSIGNMENTS

There will be approximately 10 homework assignments, which will each include problems of varying difficulty. Due dates of assignments will be announced and set typically a week after the assignments are published

### FINAL PROJECT

The final project is a more extensive written assignment that will draw on techniques acquired throughout the semester. It will be published about two weeks before the end of classes and will be due at the beginning of finals week.

### CLASS PARTICIPATION AND ATTENDANCE

Although attendance is not regularly monitored frequent absences are likely to be noted and may factor into the grade in borderline cases.

## Grading

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### COURSE SCORE

A course score will be computed from the above assessments. Homework assignments will count 70% towards the grade and the final project 30%.

**LETTER GRADES**

Letter grades will be determined based on the course score. The approximate minimum scores letter grades are 80% for an "A", 73% for an "A-", 67% for a "B+", 55% for a "B-", and 40% for a "C-". The exact cut-off scores may vary depending on the difficulty of assignments.

**Weekly Schedule**

|         |   |
|---------|---|
| Week 1  | Introduction to the probabilistic method: the first moment method                   |
| Week 2  | Lower bounds on Ramsey numbers, extremal graph theory                               |
| Week 3  | Probabilistic method with alterations: graphs with large girth and chromatic number |
| Week 4  | Second moment method I: Chebyshev's inequality and applications                     |
| Week 5  | Second moment method II: Random graphs, thresholds for subgraphs                    |
| Week 6  | Lovasz Local Lemma and applications   |
| Week 7  | Poisson paradigm I: method of moments, Stein's method                               |
| Week 8  | Poisson paradigm II: Janson's inequality and applications                           |
| Week 9  | Concentration of measure: Chernoff bounds   |
| Week 10 | Martingale methods: vertex and edge revealing filtrations, Azuma's inequality       |
| Week 11 | The phase transition in the random graph  |
| Week 12 | Correlation inequalities  |
| Week 13 | Random trees  |
| Week 14 | Random planar maps  |

**General Policies****ACADEMIC MISCONDUCT**

It is the responsibility of the Committee on Academic Misconduct to investigate or establish procedures for the investigation of all reported cases of student academic misconduct. The term "academic misconduct" includes all forms of student academic misconduct wherever committed; illustrated by, but not limited to, cases of plagiarism and dishonest practices in connection with examinations. Instructors shall report all instances of alleged academic misconduct to the committee (Faculty Rule 3335-5-487). For additional information, see the Code of Student Conduct ([http://studentaffairs.osu.edu/info\\_for\\_students/csc.asp](http://studentaffairs.osu.edu/info_for_students/csc.asp)).

**DISABILITY SERVICES**

Students with disabilities that have been certified by the Office for Disability Services will be appropriately accommodated and should inform the instructor as soon as possible of their needs. The Office for Disability Services is located in 150 Pomerene Hall, 1760 Neil Avenue; telephone 292-3307, TDD 292-0901; <http://www.ods.ohio-state.edu/>.

# Combinatorics and Graph Theory II

## Instructor and Class Information

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Lecturer:

Course Num.:

Office:

Lecture Room:

Phone:

Lecture Times:

Email:

Office Hours:

## About Course Goals

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### FORMAT

The course will meet five times a week for 55 minutes each meeting. Instructions will be mainly by lecture delivered by the instructor. It may also include occasional in-class discussion as well as short student presentations, particularly, by post-candidacy students.

### CONTENT & GOALS

This course is meant to introduce graduate students to advanced combinatorial, probabilistic, and graph theoretic methods. An emphasis is placed on covering the fundamentals of these subjects at a fast pace, emphasizing areas which are important for applications. Many open problems and areas of current research will be pointed out along the way.

### PREREQUISITES

Math 6501 or permission of instructor

## Textbook

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### MAIN REFERENCE

Reinhard Diestel: *“Graph Theory”*, Graduate Texts in Mathematics **173**. Springer; 4th ed. 2010. ISBN: 978-3642142789.

Noga Alon and Joel Spencer: *“The Probabilistic Method: Third Edition”*. Wiley, 2008. ISBN: 978-0470170205

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## Weekly Schedule

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|         |  |
|---------|--|
| Week 1  | Combinatorial designs  |
| Week 2  | Finite geometries: finite projective planes, ovoids  |
| Week 3  | Introduction to error correcting codes: sphere-packing bounds, Shannon bounds                        |
| Week 4  | Hamming codes, binary Golay codes  |
| Week 5  | Moebius inversion: inclusion-exclusion and sieve methods   |
| Week 6  | Algebraic graph theory I: adjacency matrices, Laplacians   |
| Week 7  | Algebraic graph theory II: spectral graph theory, strongly regular graphs                            |
| Week 8  | Probabilistic method I: first-moment method  |
| Week 9  | Probabilistic method II: second-moment method, concentration of measure                              |
| Week 10 | Applications of probabilistic method: existence of expanders, metric distortion                      |
| Week 11 | Association schemes: finite groups, distance regular graphs  |
| Week 12 | Combinatorics of symmetric group I: permutation statistics   |
| Week 13 | Combinatorics of symmetric group: II: symmetric functions and representation theory, Schur functions |
| Week 14 | q-series: q-Pochhammer symbol, q-analogues of combinatorial identities                               |

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